

# The opportunities elastic waves offer to soil science

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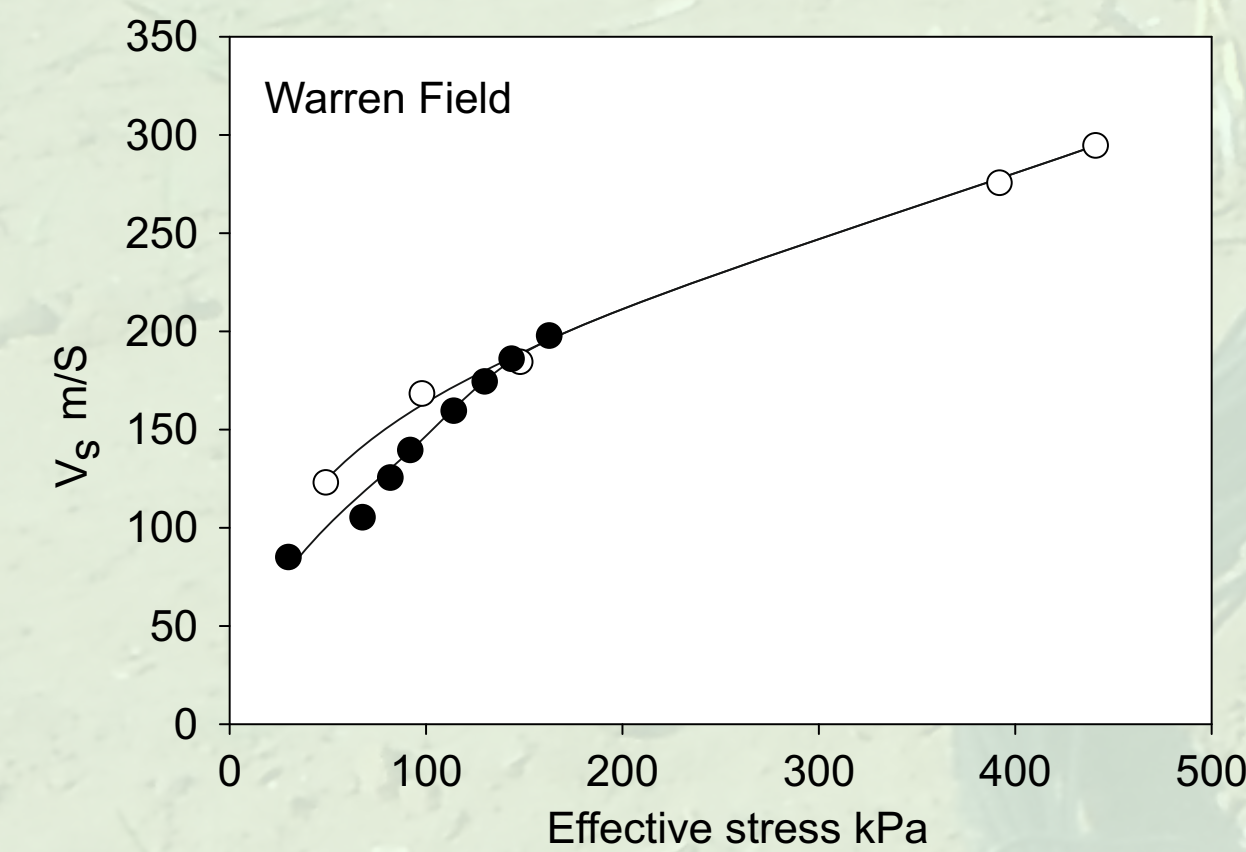
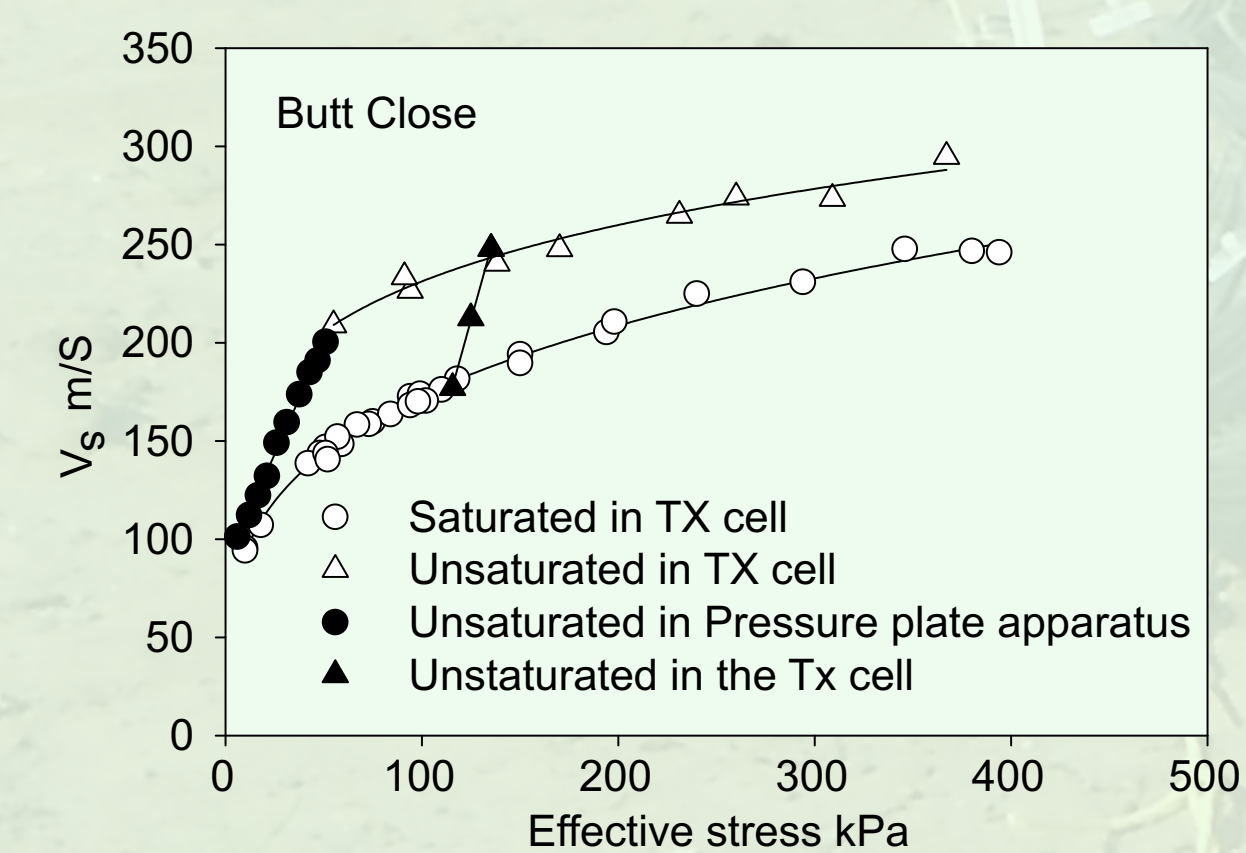
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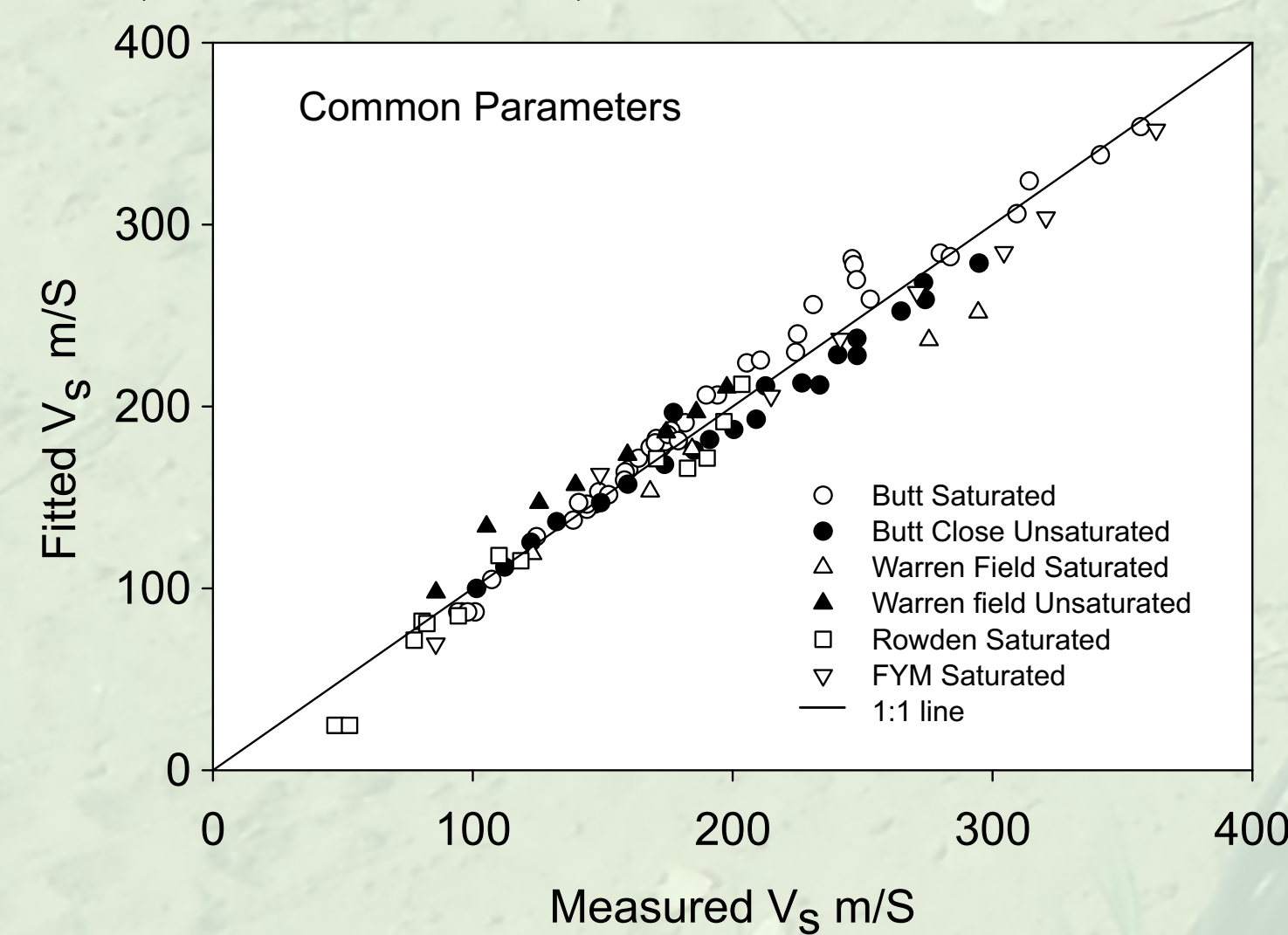
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We demonstrate the potential of a non-invasive measurement technique for the in situ monitoring of soil physical properties in the field. When soils are regarded as porous and elastic media, sub-surface wave propagation can be indicative of the soil status. Such propagation can be initiated by airborne sound through acoustic-to-seismic (A-S) coupling. Measurements of near-surface sound pressure and acoustically induced soil particle motion can be exploited to estimate the pore-related and elastic properties of soils. Measured data were compared with model predictions based on wave propagation in layered homogeneous isotropic poroelastic media described by linear Biot-Stoll theory. Soil properties were estimated through an optimization process minimizing the differences between the measurements and predictions. The fitted soil characteristics are air permeability, porosity, P-/S-wave speeds (related to bulk and rigidity moduli) and a loss factor. Layer depth was also estimated for multi-layered samples.

## Shear wave velocity



$$V_s = A \frac{(F_e - e)^{\gamma}}{1 + e} \left( \sigma_s^p - \psi \left( \frac{\psi}{\psi_{ae}} \right)^b \right)^f$$



$e$  is the void ratio  
 $F$  is the void ratio normalization factor  
 $\psi_{ae}$  is the air entry potential  
 $\psi$  is the matric potential to which the soil has dried  
 $\sigma_s$  applied stress  
 $A, r,$  and  $\gamma$  are adjustable parameters

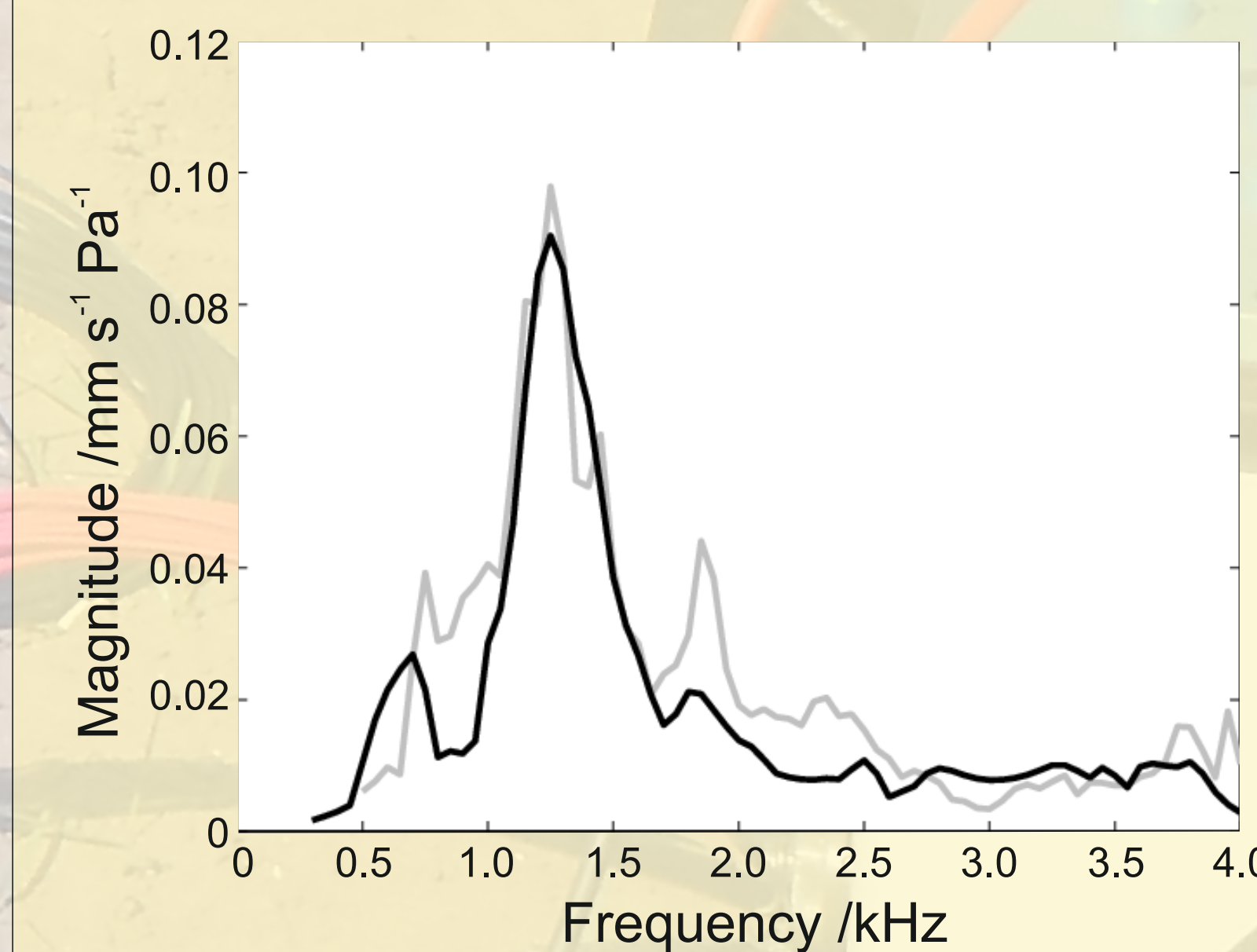
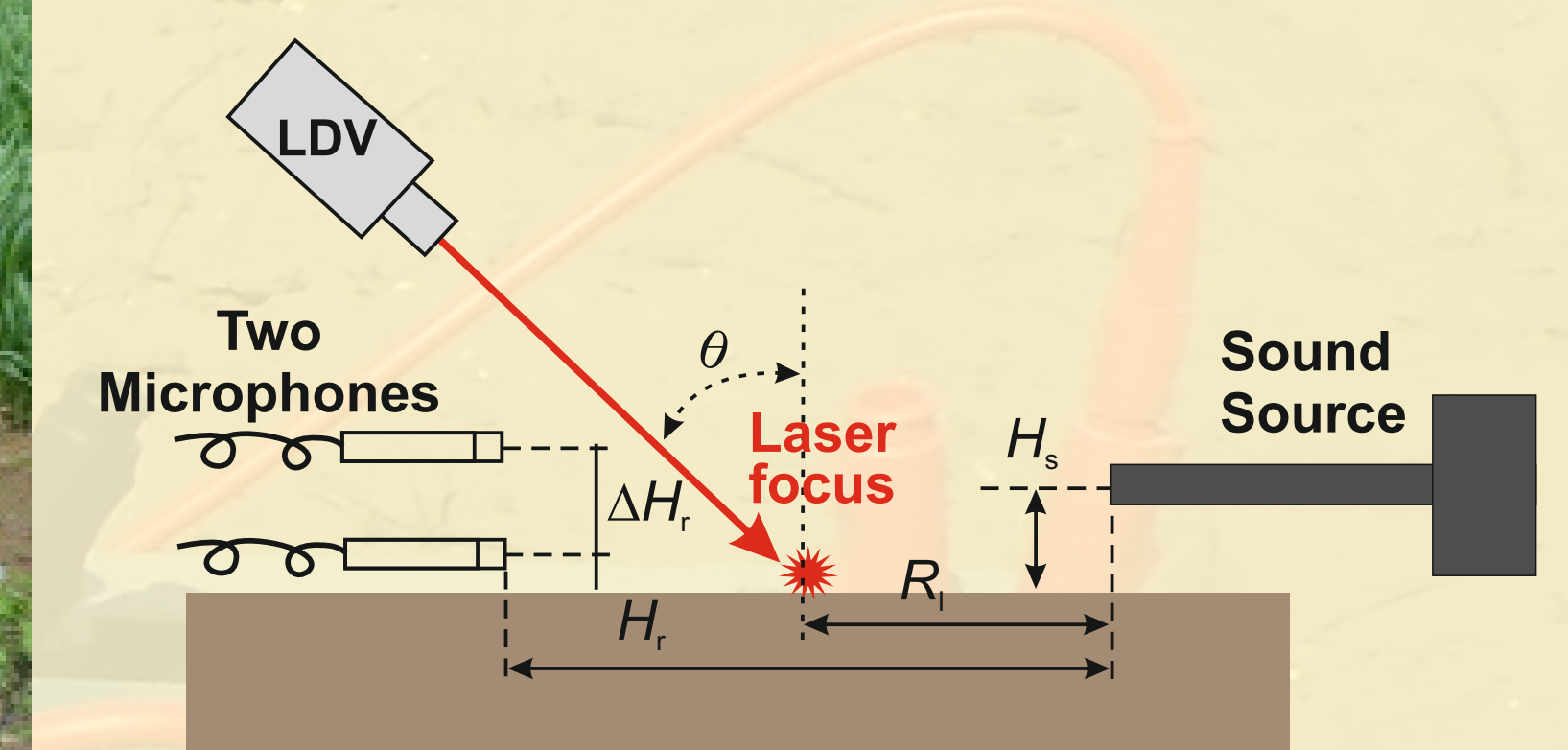
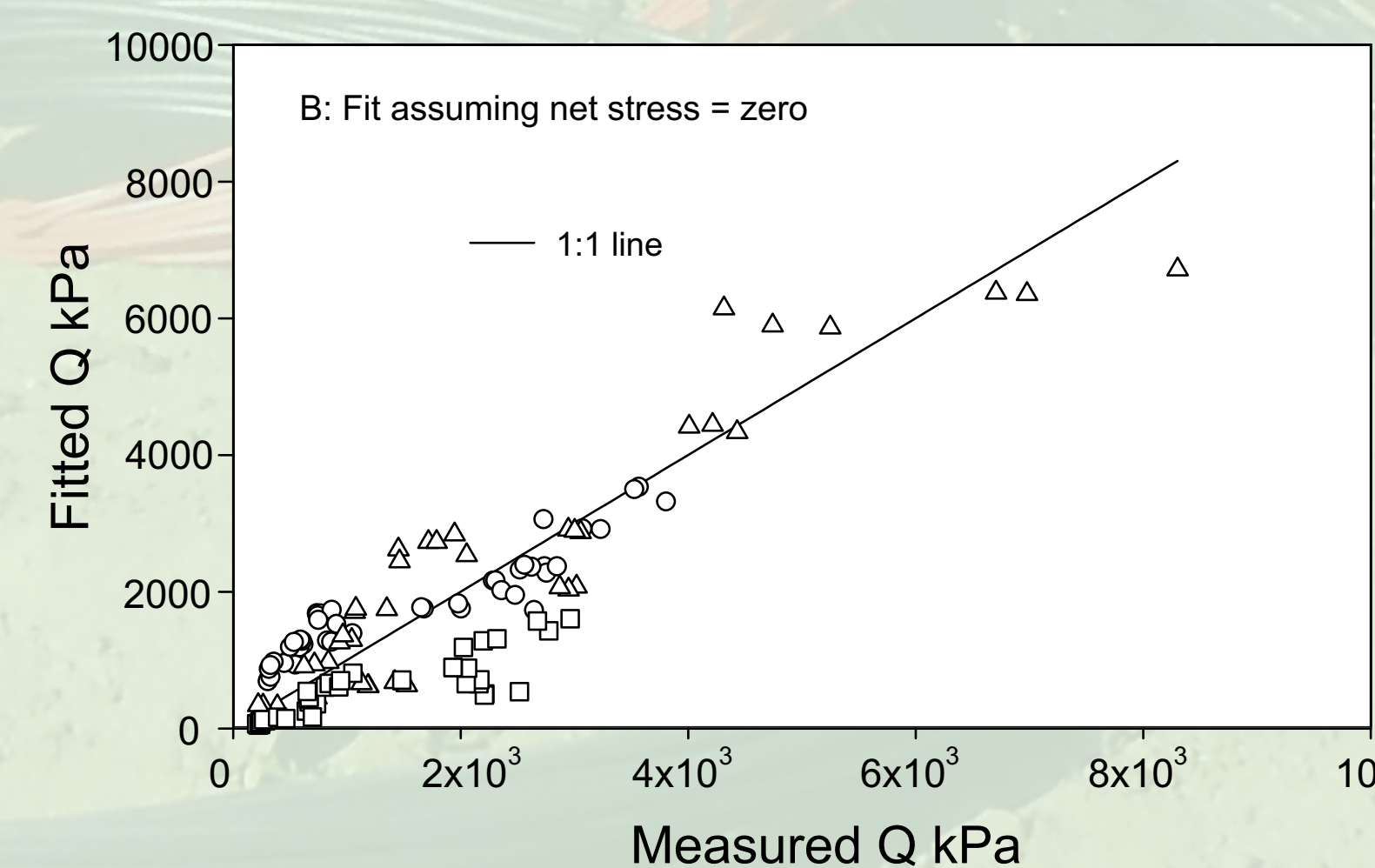
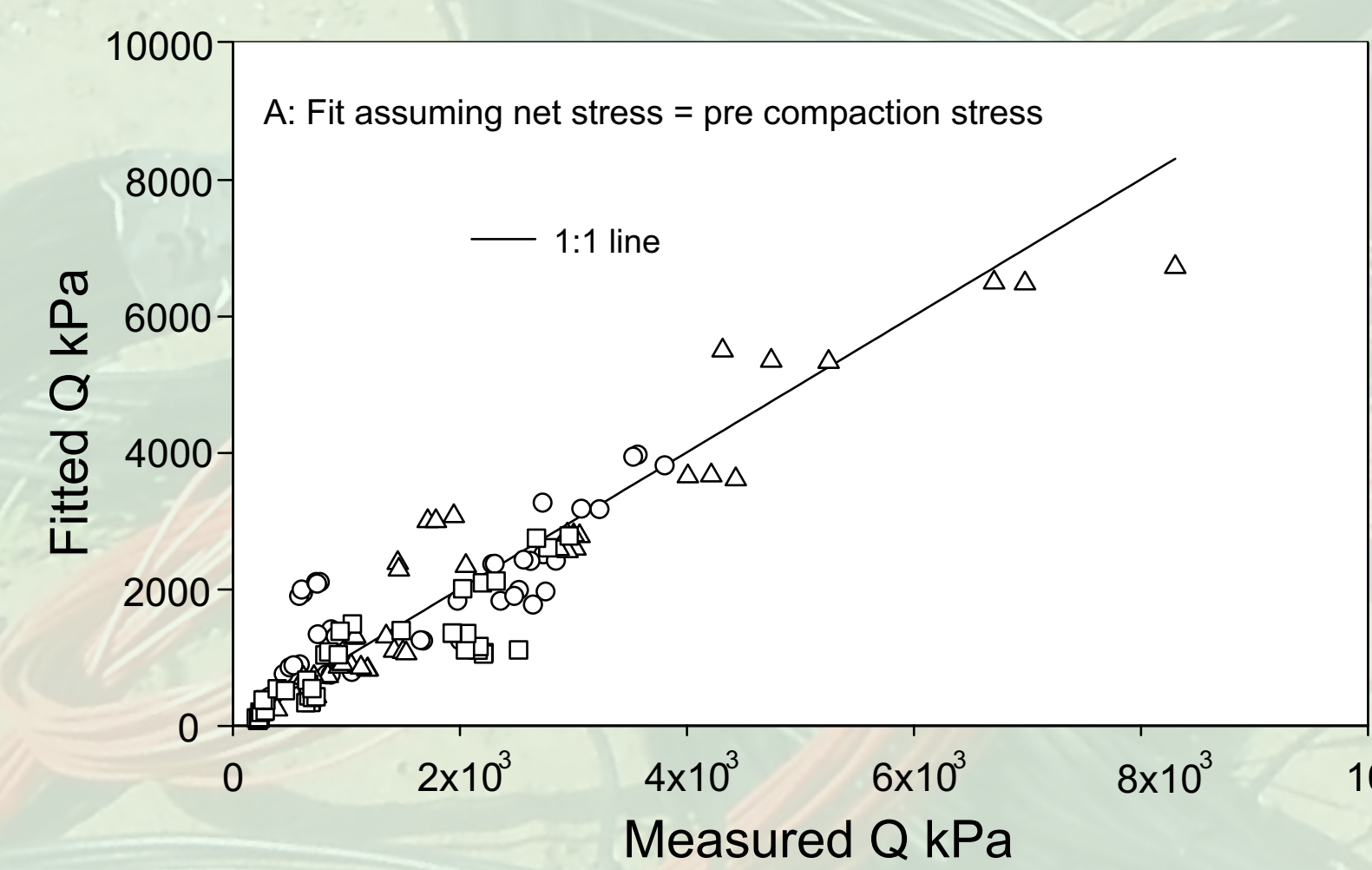
## Penetrometer resistance

On the premise that  $Q = k \rho V^2$  we fitted

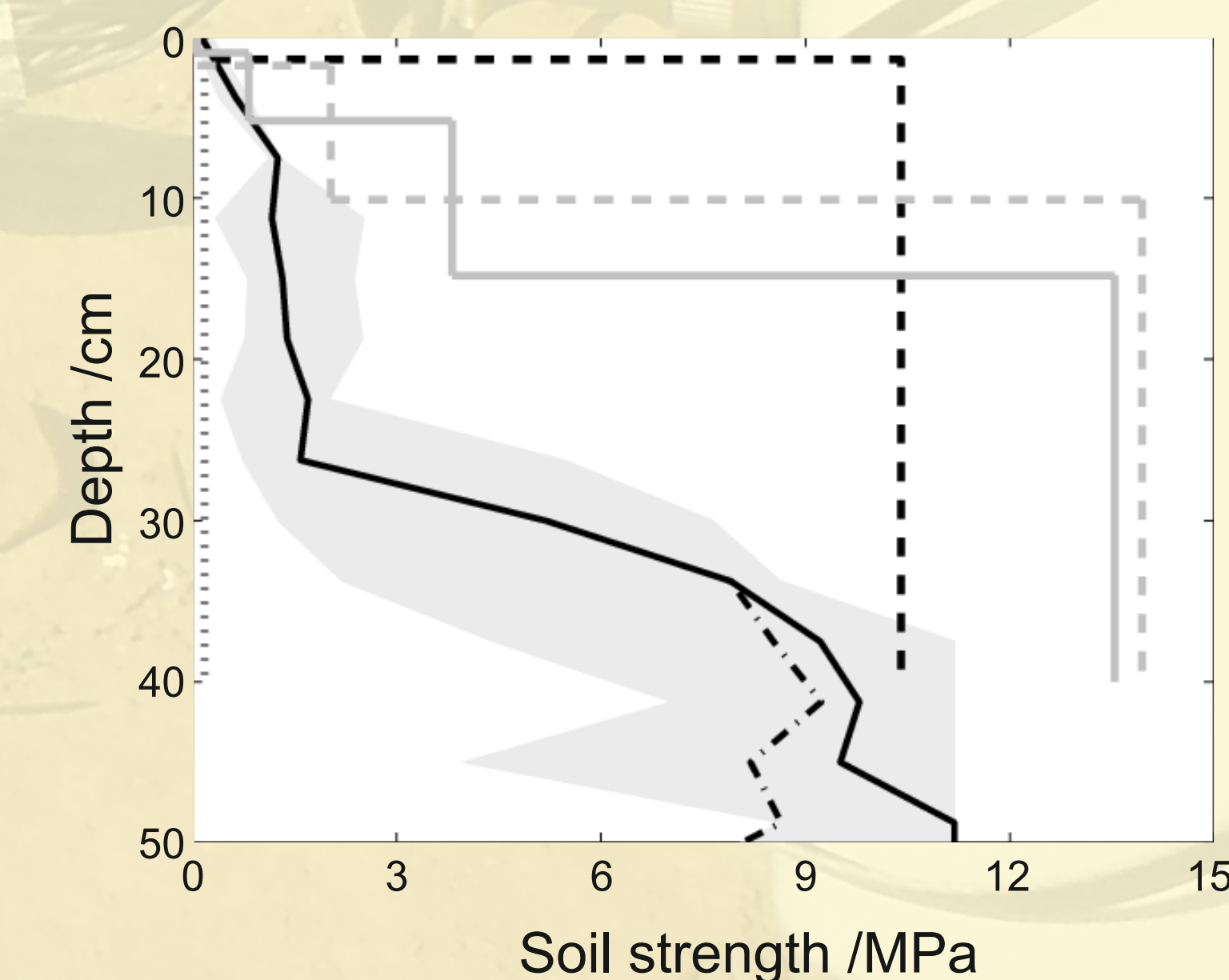
$$Q = \rho \left( A^* \frac{(F_e - e)^{\gamma}}{1 + e} \left( \sigma_s^p - \psi \left( \frac{\psi}{\psi_{ae}} \right)^b \right)^f \right)^2$$

Here  $F, A^*, p, f$  and  $b$  are empirical, adjustable parameters

$e$  is void ratio  
 $\sigma$  is the applied pressure  
 $e$  and  $\sigma$  are related with the compression characteristic  
 $\psi$  is the matric potential  
 $\psi_{ae}$  is the air entry potential



Comparisons of the measurement (in grey) and the two-layer simulation (in black) based on the deduced parameters for a cleared plot at a Rothamsted Research experimental site: (a), level difference; (b), acoustic-to-seismic coupling.



Field soil strength measured by a penetrometer and deduced by optimizations. The penetrometer data were collected in an Experimental plot 20 m away from the location of the acoustic-to-seismic measurement. The solid black line is the median of five penetrometer readings by assigning 80 kgf to the failed readings which are discarded for the separated dash/dot black line. The surrounding greyed area shows the minimum and maximum readings at each depth. The vertical dotted black line was deduced under the single-layer assumption during optimization; the dashed black line under the two-layer assumption; the dashed grey line under the three-layer assumption; the solid grey line under the four-layer assumption.