

How many test locations and replications are needed in crop variety trials for a target region?



*weikai.yan@agr.gc.ca

Weikai Yan*

Eastern Cereal & Oilseed Research Centre, AAFC, Ottawa, ON K1A 0C6

Introduction

- Crop variety trials are essential for plant breeders to select and for agronomists to recommend crop cultivars to growers.
- How many test locations and replications are needed in crop variety trials are questions everyone conducting variety trials has to ask.
- The purpose of this work was to develop simple formulas for estimating the optimum number of replicates within a trial and the optimum number of test locations for a target region.

The optimum number of replications within a trial

▶ The effectiveness of variety trials is measured by the heritability achieved in them. The solution for the optimum numbers resides in the definitions of heritability.

▶ The heritability within a trial is determined by (DeLacy et al, 1996):

$$H = \frac{\sigma_g^2}{\sigma_g^2 + \frac{\sigma_e^2}{N_r}}$$

▶ where H is the heritability of the trial for the trait of interest, σ_g^2 is the genotypic variance, σ_e^2 the error variance, and N_r the number of replicates in the trial. This formula can be written as:

$$N_r = \left(\frac{\sigma_e^2}{\sigma_g^2} \right) \frac{H}{1-H} = Q_r \frac{H}{1-H}$$

▶ The relationships between N_r and H is depicted in Figure 1. The increase in the number of replications N can effectively improve H only when H is smaller than certain level, say $H = 0.75$, beyond which the effect gradually diminishes.

▶ Assuming $H = 0.75$ is the target trial heritability, the number of replicates needed is determined by

$$N_{r,H=0.75} = 3 \left(\frac{\sigma_e^2}{\sigma_g^2} \right) \frac{H}{1-H} = 3Q_r \quad [1]$$

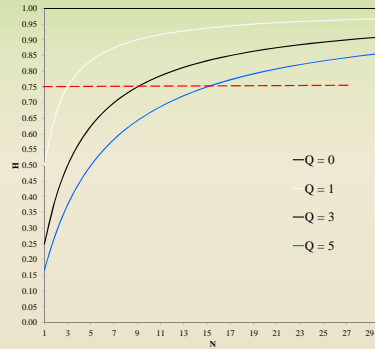


Fig. 1. Relationship between trial heritability (H) and number of replications at different trial noise levels (Q)

The optimum number of test locations for a target region

• Likewise, the heritability at multilocation trial level is defined as:

$$H = \frac{\sigma_g^2}{\sigma_g^2 + \frac{\sigma_{ge}^2}{N_e} + \frac{\sigma_e^2}{N_e N_r}}$$

• where σ_g^2 is the genotypic variance, σ_e^2 the experimental error variance, σ_{ge}^2 the genotype-by-location interaction variance, N_e the number of test locations, and N_r the number of replicates within trials. This equation can be written as:

$$N_e = \left[\frac{\sigma_{ge}^2 + \sigma_e^2 / N_r}{\sigma_g^2} \right] \frac{H}{1-H}$$

• Given the relationship between H and N_e (Fig. 1), the number of test locations needed to achieve $H = 0.75$ may be considered as the optimum number of test locations for a target region and can be determined by

$$N_{e,H=0.75} = 3 \left[\frac{\sigma_{ge}^2 + \sigma_e^2 / N_r}{\sigma_g^2} \right] = 3Q_e$$

• Assuming each trial is properly replicated this formula can be simplified to:

$$N_{e,H=0.75} = 1 + 3 \left(\frac{\sigma_{ge}^2}{\sigma_g^2} \right) \quad [2]$$

Case study

Table 1. Number of replicates used (N) and number of replicates needed to achieve a heritability of 0.75 (N_{H75}) estimated using Eq. [1] for different traits in the oat registration trials at Ottawa, Ontario from 2008 to 2012.

Year	Number of Reps	Days to heading	Plant Height	Test weight	1000-kernel weight	Grain yield
2008	N	4.0	4.0	3.9	3.9	4.0
	N_{H75}	4.0	2.1	1.7	1.5	1.4
2009	N	2.0	4.0	4.0	4.0	4.0
	N_{H75}	2.5	1.4	2.3	1.6	4.1
2010	N			4.8	4.8	4.8
	N_{H75}			1.8	1.3	1.8
2011	N	6.0	6.0	6.0	5.9	5.9
	N_{H75}	1.4	2.6	1.5	2.1	2.4
2012	N	6.0	6.0			6.0
	N_{H75}	2.2	3.0			3.1
Mean	N	4.5	5.0	4.7	4.7	5.0
	N_{H75}	2.5	2.3	1.8	1.6	2.6

Table 2 Number of test locations used (N) and number of test locations needed to achieve an $H = 0.75$ (N_{H75}) estimated using Eq. [2] for oat grain yield within each of two mega-environments in eastern Canada.

Year	Number of Locations	Southern mega-environment	Northern mega-environment
2006	N	4.0	5.0
	N_{H75}	7.6	5.1
2007	N	4.0	6.0
	N_{H75}	6.2	2.3
2008	N	5.0	8.0
	N_{H75}	4.8	6.6
2009	N	5.0	5.0
	N_{H75}	10.1	5.6
2010	N	5.0	5.0
	N_{H75}	27.7	8.8
2011	N	4.0	4.0
	N_{H75}	18.3	6.5
2012	N	3.0	4.0
	N_{H75}	9.0	4.5
Mean	N	4.3	5.3
	N_{H75}	12.0	5.6

References

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